



Algebraic:

$$j = \sqrt{-1}$$

$$j = \frac{-1}{j}$$

$$\text{sinc}(x) = \frac{\sin(\pi x)}{\pi x}$$

Euler Identities:

$$e^{j\theta} = \cos(\theta) + j \sin(\theta)$$

$$\cos(\theta) = \frac{e^{j\theta} + e^{-j\theta}}{2}$$

$$\sin(\theta) = \frac{e^{j\theta} - e^{-j\theta}}{2j}$$

Exponential Fourier Series:

$$C_n = \frac{1}{T} \int_{t_1}^{t_1+T} x(t) e^{-jn\omega_0 t} dt \quad n = 0, \pm 1, \pm 2, \dots$$

$$x(t) = \sum_{n=-\infty}^{\infty} C_n e^{jn\omega_0 t}$$

where $\omega_0 = 2\pi/T$

Trigonometric Fourier Series:

$$A_n = \frac{2}{T} \int_{t_1}^{t_1+T} x(t) \cos(n\omega_0 t) dt \quad n = 0, 1, 2, \dots$$

$$B_n = \frac{2}{T} \int_{t_1}^{t_1+T} x(t) \sin(n\omega_0 t) dt \quad n = 0, 1, 2, \dots$$

$$x(t) = \frac{A_0}{2} + \sum_{n=1}^{\infty} A_n \cos(n\omega_0 t) + B_n \sin(n\omega_0 t)$$

Fourier Transform and Inverse

$$\mathcal{F}\{x(t)\} = X(\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$$

$$\mathcal{F}^{-1}\{X(\omega)\} = x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) e^{j\omega t} d\omega$$