

## Chapter 7

7-1

$$\text{error} = \lim_{s \rightarrow 0} sR(s)/(1+G(s))$$

for step ( $R(s) = 1/s$ ), error = 0

for ramp ( $R(s) = 1/s^2$ ), error = 0

for  $50t^2$  ( $R(s) = 100/s^3$ ), error = 0.43

7-3

Reduce to an equivalent unity feedback system

$$G(s) = \frac{5}{s^2 + 16s + 15}$$

$$\text{and } \lim_{s \rightarrow 0} G(s) = K_p = 1/3$$

finally, the error due to  $15 u(t)$  is  $15 * 1/(1+K_p) = 11.25$

7-4

This system is of type 0. Using the table, we quickly find

ramp error = Infinity

parabola error = Infinity

$$\text{and for } 35 u(t), \text{ error} = 35 * 1/(1+K_p) = 7$$

7-9

The closed loop transfer function is found to be

$$T(s) = \frac{1250}{s^2 + 50s + 1250}$$

from which we can find  $\omega_n = \sqrt{1250}$ , and  $\zeta = .707$

a) The overshoot is therefore 4.32%

b)  $T_s = 4/\zeta * \omega_n = .16$  s

c) error step = 0, it is a type 1 system.

d)  $K_v = 25$ , and error ramp =  $5 * (1/25) = .2$

e) error parabola = Infinity.

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7-14

This can be simplified to the unity feedback system with

$$G(s) = \frac{5s + 10}{2s(s+1)}$$

This is a type 1 system because of the  $2s$ .