

31

We will reflect all impedances to the middle (Theta 2), since we wish to find the transfer function  $O_2(s)/T(s)$ .

The following reflections are made:

$T(s)$  reflects to  $T(s) \cdot (12/4) = 3 T(s)$   
 $J_1$  reflects to  $J_1 \cdot (12/4)^2 = 9 J_1$   
 $D_1$  reflects to  $D_1 \cdot (12/4)^2 = 9 D_1$   
 $D_3$  reflects to  $D_3 \cdot (4/16)^2 = D_3/16$   
 $J_3$  reflects to  $J_3 \cdot (4/16)^2 = J_3/16$   
 $K$  reflects to  $K \cdot (4/16)^2 = K/16$

We then have a total  $J$  of

$$J_{total} = 9 J_1 + J_2 + J_3/16 = 20$$

And analogously,

$$D_{total} = 9 D_1 + D_2 + D_3/16 = 13$$

$$K_{total} = K/16 = 4$$

We can then write the equation of motion as

$$O_2(s) \cdot [J_{total} s^2 + D_{total} s + K_{total}] = 3 T(s), \text{ or}$$

$$\frac{O_2(s)}{T(s)} = \frac{3}{20s^2 + 13s + 4}$$

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32

We will once again reflect the impedances to  $O_2(s)$ , since it is the output in question.

We then find that

$$O_2(s)[200 + 3 \cdot (50/5)^2]s^2 + 1000s + 250(50/5 \cdot 5/25)^2 = T(s) \cdot (50/5)$$

Note that the spring,  $k$ , was reflected through two sets of gears, the  $(5/25)^2$  term and the  $(50/5)^2$ .

It is clear now that

$$\frac{O_2(s)}{T(s)} = \frac{(1/50)}{s^2 + 2s + 2}$$

A second order system!

33. One can show that the transfer function is

$$.8/(s+1)$$